



College of Computing and Mathematics  
Department of Mathematics

**MATH531 – Real Analysis**  
**SYLLABUS**  
AY 2022-2023 (Term 222)

<b>Instructor</b>	Dr. Khairul Saleh	<b>Phone</b>	+966-13-860-7524
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<b>Office Hour</b>	09:00 PM – 09:45 PM (Sun, Tue) 09:30 AM – 10:30 AM (Mon, Wed) and by appointment		

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**Textbook** *Real Analysis* by H.L. Royden and P.M. Fitzpatrick, Fourth Edition, Pearson

**Description** *Lebesgue measure and outer measure. Measurable functions. The Lebesgue integral. Lebesgue convergence theorem. Differentiation and integration.  $L^p$  spaces. Riesz representation theorem. Introduction to Banach and Hilbert spaces.*

**Objectives** *The course is designed to introduce graduate students to measure theory, which particularly focusing on the Lebesgue measure, integration, and the classical  $L^p$  spaces.*

**Learning Outcomes** *Upon successful completion of this course, a student should be able to:*

- (1) Identify the Lebesgue Measurable sets and describe basic properties of the Lebesgue measure.*
- (2) Perform operations on measurable functions.*
- (3) Use the Monotone Convergence Theorem, Fatou's Lemma, Fubini's Theorem, and the Dominated Convergence Theorem.*
- (4) Compare the Riemann integral and the Lebesgue integral.*
- (5) Distinguish different types of convergences.*
- (6) Identify functions of bounded variations and absolutely continuous functions.*
- (7) Use basic properties of the  $L^p$  spaces.*

Week	Date	Topic
1	15 – 19 Jan	2.1 Introduction 2.2 Lebesgue outer Measure 2.3 The $\sigma$ -Algebra of Lebesgue Measurable sets
2	22 – 26 Jan	2.4 Outer and Inner Approximation of Lebesgue Measurable 2.5 Countable Additivity, Continuity, and the Borel-Cantelli Lemma
3	29 Jan – 2 Feb	3.1 Sums, Products, and Compositions 3.2 Sequential Pointwise Limits and Simple Approximation
4	5 – 9 Feb	3.3 Littlewood's Three Principles, Egoroff's Theorem, and Lusin's Theorem 4.1 The Riemann Integral
5	12 – 16 Feb	4.2 The Lebesgue Integral of a Bounded Measurable Function over a Set of Finite Measure 4.3 The Lebesgue Integral of a Measurable Nonnegative Function
6	19 – 21 Feb	4.4 The General Lebesgue Integral 4.5 Countable Additivity and Continuity of Integration
<b>Saudi Founding Day (22 – 23 February 2023)</b>		
<b>Major Exam 1. Material: 2.1-4.4. Date: 26 February 2023. Time: TBA</b>		
7	26 Feb – 2 Mar	4.6 Uniform Integrability: The Vitali Convergence 5.1 Uniform Integrability and Tightness: A General Vitali Convergence Theorem
8	5 – 9 Mar	5.2 Convergence in Measure 5.3 Characterizations of Riemann and Lebesgue Integrability
9	12 – 16 Mar	6.1 Continuity of Monotone Functions 6.2 Differentiability of Monotone Functions: Lebesgue's Theorem
10	19 – 23 Mar	6.3 Functions of Bounded Variation: Jordan's Theorem 6.4 Absolutely Continuous Functions
11	26 – 30 Mar	6.5 Integrating Derivatives: Differentiating Indefinite Integrals 6.6 Convex Functions
12	2 – 6 Apr	7.1 Normed Linear Spaces 7.2 The Inequalities of Young, Holder, and Minkowski
<b>Major Exam 2. Material: 4.5-6.6. Date: 6 April 2023. Time: TBA</b>		
13	9 – 13 Apr	7.3 $L^p$ is Complete: The Riesz-Fischer Theorem 17.1 Measures and Measurable Sets
<b>Eid Al-Fitr Holidays (16 – 27 April 2023)</b>		
14	30 Apr – 4 May	17.2 Signed Measures: The Hahn and Jordan Decompositions 18.1 Measurable Functions
15	7 – 11 May	18.2 Integration of Nonnegative Measurable Functions Review
<b>Final Exam: Comprehensive. Date: TBD</b>		

**Grading Policy:**

- Major Exam 1 25%
- Major Exam 2 25%
- Homework Assignment 15%
- Final Exam (Comprehensive) 35%